

Mathematics (Senior Secondary)

1. Introduction

The Department of Mathematics at HKUGAC strives to develop students' mathematical skills, their ability to communicate mathematics, their ability to reflect and evaluate, and their ability to develop and apply mathematical and technical knowledge. We aim to foster in our students a positive attitude, an appreciation of mathematics and their significance to everyday life. The programme will incorporate elements to increase intercultural awareness and cross-subject links.

The curriculum is designed in accordance with the syllabus for Secondary 4 – 6 Mathematics, using the approaches in compliance with the New Senior Secondary Curriculum and Assessment Guides in Mathematics Education, the general guidelines set by the Curriculum Development Council and the Hong Kong Examinations and Assessment Authority in 2007.

1.2 Teaching methods

Given students' diverse learning styles, we employ various teaching and assessment strategies to ensure that all of our students have an opportunity to learn and demonstrate their understanding.

The teacher will act as a resource for the student to learn to use. This will require them to take an active part in their own learning. Thus, they are encouraged to ask questions when there is a conflict between their understanding and the feedback that they obtain.

Local and international cultures, as well as the history of mathematics, are incorporated into the syllabus wherever possible. Throughout the six years of study, students will be assigned problem solving tasks, various projects and modelling assignments that will require them to apply their mathematical knowledge to applications involving problems from the real world.

The use of e-resources and technology is incorporated into the curriculum in order to facilitate mathematical learning and assessment. Technology, whenever appropriate, is used in lessons for students to explore mathematical concepts, to be assessed and to perform mathematical experiments. Learning materials are also provided online.

We will provide various levels of study groups to ensure that all students are given the academic opportunity and challenge to reach their full potential. This is essential in developing students' abilities to express ideas clearly and to think critically, in order for them to become contributing members to society.

For the higher ability students, we provide extra training for them to take part in the International Mathematical Olympiad.

1.3 Assessment

Assessment will take various forms that will incorporate skills acquisition, class participation, oral discussion, note-taking, worksheets, assignments, projects and written tests.

2. Aims & Objectives of Mathematics Education

The aims for mathematics are to enable students to:

- develop a positive attitude toward the continued learning of mathematics
- appreciate the usefulness, power and beauty of mathematics, and recognize its relationship with other disciplines with everyday life
- gain knowledge and develop understanding of mathematical concepts
- develop mathematics skills and apply them in daily life
- develop the ability to communicate mathematics with appropriate symbols and language
- develop ability to reflect upon and evaluate the significance of their work and the work of others
- share ideas and experience and work cooperatively with others in accomplishing mathematical tasks/activities and solving mathematical problems
- develop patience and persistence when solving mathematical problems
- develop and apply information and communication technology skills in the study of mathematics
- appreciate the international dimensions of mathematics and its varied cultural and historical perspectives

At the end of the course students should be able to:

- know and understand concepts, and demonstrate skills, from the branches of mathematics
- understand and use a variety of mathematical forms and have the ability to move confidently between them
- select and use appropriate mathematical knowledge, skills and techniques when investigating problems and justify their relationship
- recognize patterns and structures and describe them as relationships or general rules when investigating problems

- draw conclusions consistent with findings
- communicate mathematical facts, ideas, methods, results and conclusions using appropriate language and symbols
- reflect on their methods and processes and be able to consider possible alternative approaches
- evaluate the significance and reliability of their findings and findings of others

3. Curriculum

3.1 Mathematics Curriculum Framework

| 9 Refined Generic Skills [#] | | |
|--|--------------------------|---|
| Basic Skills: Communication Skills, Mathematical Skills, IT Skills | | |
| Thinking Skills: Critical Thinking Skills, Creativity, Problem Solving Skills | | |
| Personal and Social Skills: Self-management Skills, Self-learning Skills, Collaboration Skills | | |
| Level | Dimensions | Units |
| S4 | Number and Algebra | Number Systems Quadratic Equations in One Unknown Basic Knowledge of Functions Quadratic Functions More about Polynomials Exponential Functions Logarithmic Functions Rational Functions |
| | Measure, Shape and Space | Equations of Straight Lines Basic Properties of Circles More about Basic Properties of Circles Basic Trigonometry Mensuration |
| | Data Handling | Nil |

| | | |
|----|--------------------------|---|
| | Module 1 | Binomial Expansion Exponential Functions and Logarithmic Functions Limits and Derivatives Differentiation |
| | Module 2 | Pre-requisite Knowledge Mathematical Induction Binomial Theorem More about Trigonometric Functions Limits and the Number e |
| S5 | Number and Algebra | More about Equations Inequalities in One Unknown More about Graphs of Functions Variations |
| | Measure, Shape and Space | Equations of Circles Locus Solving Triangles Applications in Trigonometry |
| | Data Handling | Permutation and Combination More about Probability Measures of Dispersion More about Dispersion |
| | Module 1 | Applications of Differentiation Indefinite Integration and its Applications Definite Integration Applications of Definite Integration Further Probability Probability Distribution, Expectation and Variance Discrete Probability Distributions |

| | | |
|----|--------------------------|---|
| | Module 2 | Differentiation Applications of Differentiation Indefinite Integration Definite Integration Applications of Definite Integration Matrices and Determinants |
| S6 | Number and Algebra | Arithmetic Sequences Geometric Sequences Linear Inequalities in Two Unknowns and Linear Programming |
| | Measure, Shape and Space | Nil |
| | Data Handling | Uses and Abuses of Statistics |
| | Module 1 | The Normal Distribution and its Applications Sampling Distribution and Point Estimation Interval Estimation |
| | Module 2 | Systems of Linear Equations Introduction to Vectors Scalar Products and Vector Products |

3.2 Delivery Schedule

S4

| Time Frames | Compulsory Part | Module 1 | Module 2 |
|--------------------|---|--|---|
| September | Equations of Straight Lines, Number Systems | Nil | Nil |
| October | Quadratic Equations in One Unknown, | | |
| November | Basic Knowledge of Functions Quadratic Functions | | |
| December | More about Polynomials | Nil | Nil |
| January | First Term Exam | | |
| February | Exponential Functions, Logarithmic Functions, | Binomial Expansion , Exponential Functions and Logarithmic Functions | Pre-requisite Knowledge, Mathematical Induction |
| March | Rational Functions, Basic Trigonometry, | Limits and Derivatives | Binomial Theorem |
| April | Basic Properties of Circles, More about Basic Properties of Circles | Differentiation | More about Trigonometric Functions |
| May | Revision of Mensuration, Law of Indices, Change of Subject, Factorization | | Limits and the Number e |
| June | Final Exam | Final Exam | Final Exam |
| July | Summer Holidays | Summer Holidays | Summer Holidays |

| Time Frames | Compulsory Part | Module 1 | Module 2 |
|--------------------|---|---|--------------------------------------|
| September | More about Equations, Inequalities in One Unknown | Applications of Differentiation | Differentiation |
| October | More about Graphs of Functions, Variations | Indefinite Integration and its Applications | Applications of Differentiation |
| November | Permutation and Combination | Definite Integration | |
| December | More about Probability | Applications of Definite Integration | Indefinite Integration |
| January | Frist Term Exam | First Term Exam | First Term Exam |
| February | Solving Triangles, Applications in Trigonometry | Further Probability | Definite Integration |
| March | Measures of Dispersion, More about Dispersion | Probability Distribution, Expectation and Variances | Applications of Definite Integration |
| April | IGCSE | Discrete Probability Distributions | Matrices and Determinants |
| May | Locus, Equations of Circles | | |
| June | Final Exam | Final Exam | Final Exam |
| July | Summer Holidays | Summer Holidays | Summer Holidays |

| Time Frames | Compulsory Part | Module 1 | Module 2 |
|--------------------------|---|---|--|
| September | Arithmetic Sequences Geometric Sequences | The Normal Distribution and its Applications | Systems of Linear Equations |
| October | Linear Inequalities in Two Unknowns and Linear Programming Uses and Abuses of Statistics | Sampling Distribution and Point Estimation Interval Estimation | Introduction to Vectors Scalar Products and Vector Products |
| November | Assessment week | | |
| - December | Revision | | |
| January | Mock Exam | | |
| February | Post-Exam Revision Programme | | |
| March - April | Study Leave | | |
| May | HKDSE | | |

4. Assessing students

4.1 Formative and Summative Assessment

Formative assessment is an integral part of the learning experience that is designed to measure what students know and what they are learning as they go along; the objectives addressed by specific assessment tasks are shared with students, with feedback taking place. Formative assessment is carried out in various ways, including project work, oral presentation, class discussions, homework assignments, and written tests in class or at home. Summative assessment is the judgment made by the teacher of the standard of achievement reached by each student at a particular point in time and at the end of the year.

4.2 Weighting of Component Parts

| | S4 – S5 | S6 |
|------------------------------------|---------|------|
| Continuous Assessment [#] | 40% | 40% |
| First Term Exam | 30% | - |
| Final Exam | 30% | - |
| Mock Exam | - | 60% |
| Total | 100% | 100% |

[#] Continuous Assessment includes homework, quizzes and unit tests.

4.3 Assessment Criteria

Compulsory Part

The students are assessed on three assessment criteria:

“Numerical and Algebraic Skills” (NAS); “Spatial and Geometric Skills” (SGS);

“Data Handling Skills” (DHS)

“Application of Mathematical Concepts and Skills” (AM).

S4

| Assessment Criteria | Topics involved | |
|---------------------|---|--|
| | S4 Term 1 | S4 Term 2 |
| NAS | <ul style="list-style-type: none"> • Number Systems • Quadratic Equations in One Unknown • Basic Knowledge of Functions • Quadratic Functions • More about Polynomials | <ul style="list-style-type: none"> • Exponential Functions • Logarithmic Functions • Rational Functions |
| SGS | <ul style="list-style-type: none"> • Equations of Straight Lines | <ul style="list-style-type: none"> • Basic Trigonometry • Basic Properties of Circles • More about Basic Properties of Circles • Mensuration** |
| DHS | Not assessed | Not assessed |

** This topic is a revision of relevant content learnt in junior forms

S5

| Assessment Criteria | Topics involved | |
|---------------------|---|---|
| | S5 Term 1 | S5 Term 2 |
| NAS | <ul style="list-style-type: none"> • More about Equations • Inequalities in One Unknown • More about Graphs of Functions • Variations | Not assessed |
| SGS | Not assessed | <ul style="list-style-type: none"> • Solving Triangles • Application in Trigonometry • Locus • Equations of Circles |
| DHS | <ul style="list-style-type: none"> • Permutation and Combination • More about Probability | <ul style="list-style-type: none"> • Measures of Dispersion • More about Dispersion |

S6

| Assessment Criteria | Topics involved |
|---------------------|---|
| | S6 Term 1 |
| NAS | <ul style="list-style-type: none"> • Arithmetic Sequences • Geometric Sequences • Linear Inequalities in Two Unknowns and Linear Programming |
| SGS | Not assessed |
| DHS | <ul style="list-style-type: none"> • Uses and Abuses of Statistics |
| AM | <ul style="list-style-type: none"> • Cross-topic assessment |

Extended Part – Module 1

S4 Term 2

1. Manipulation of Binomial Expansions; Exponential and Logarithmic Functions
2. Computation of Limits and Derivatives of Different Functions

S5 Term 1

1. Application of Differentiation and Indefinite Integration Techniques to Solve Real-Life Problems
2. Computation and Application of Definite Integrals to Solve Real-Life Problems

S5 Term 2

1. Solving Problems about Conditional Probability and Random Variables
2. Modelling Real-Life Scenarios by Discrete Distributions

S6 Term 1

1. Modelling Real-Life Scenarios by the Normal Distribution
2. Estimation of Parameters from Samples and Construction of Confidence Intervals

Extended Part – Module 2

S4 Term 2

1. Manipulation of Mathematical Induction
2. Manipulation of Binomial Theorem
3. Manipulation of More about Trigonometric Functions
4. Computation of Limit and the number e

S5 Term 1

1. Computation of Differentiation
2. Computation of Application of Differentiation
3. Computation of Indefinite Integration

S5 Term 2

1. Computation of Definite Integration
2. Techniques and Application of Definite Integration
3. Manipulation of Matrices and Determinants

S6 Term 1

1. Exploration of System of Linear Equations by Matrices
2. Introduction to Vectors
3. Computation of Scalar Products and Vector Products

4.4 Reference Level Descriptors and Boundaries

| Levels | Boundaries of Levels | |
|--------|----------------------|----------------------|
| | Compulsory Part | Module 1 or Module 2 |
| 5** | 90% or above | 90% or above |
| 5* | 85% to 89% | 80% to 89% |
| 5 | 75% to 84% | 70% to 79% |
| 4 | 65% to 74% | 60% to 69% |
| 3 | 50% to 64% | 50% to 59% |
| 2 | 35% to 49% | 35% to 49% |
| 1 | 34% or below | 34% or below |

The marks are rounded off to the nearest %.

The actual boundaries will vary depending on the performance of students.

4.5 Requirement of taking the extended module in S4 to S6

Based on our experiences of our graduates' past performances in the HKDSE, if students cannot achieve a satisfactory standard in the school examinations they tend to struggle to keep up in the compulsory part and the extended module in Mathematics. In order to help students focus on the compulsory part and obtain a better grade in the HKDSE, we have set the following benchmarks that students must meet if they wish to continue taking M1 or M2:

| | Benchmark | |
|--------------------|-----------------|--------------------------|
| | Compulsory Part | Extended Part (M1 or M2) |
| S4 First Term Exam | 50% or above | - |
| S4 Final Exam | 60% or above | 40% or above |
| S5 First Term Exam | | |
| S5 Final Exam | | |

5. Parents' role and homework and assignments

5.1 Parents' role

Parents are encouraged to talk to their children about their work in class, what they are currently learning and check the aims and objectives of the unit being studied. They should also discuss the results obtained by their children and to regularly check their diaries.

Homework is a valuable aid to help students make the most of their school experience. Homework consolidates, reinforces and strengthens concepts learnt in class, encourages students to develop responsibility, time management skills, good study habits and helps teachers assess the performance of students. Teachers will assign homework at a suitable level of difficulty and related appropriately to specific objectives. A homework load of around 30 minutes will be assigned on the day of each mathematics lesson.

5.2 Homework Policy

As a measure to train students to be responsible for completing homework in a timely manner, late submission will result in zero marks given. Students who hand in homework late will be required to complete the unfinished work after school and the homework will receive their teachers' feedback as usual.